## Do You Know?

If you can solve nearly all of the following problems with little difficulty, then the Art of Problem Solving textbook Introduction to Algebra would only serve as a review for you.

1. A box containing 3 oranges, 2 apples, and one banana weighs 15 units. Another box containing 5 oranges, 7 apples, and 2 bananas weighs 44 units. A third box containing 1 orange, 3 apples, and 5 bananas weighs 26 units. How much does each fruit weigh?
2. The expression $x^{5}+y^{5}$ can be written as the product of $x+y$ and another factor. Find that other factor.
3. If $x=\frac{1-i \sqrt{3}}{2}$, then what is $\frac{1}{x^{2}-x}$ ?
4. Find all values of $z$ such that $z^{4}-4 z^{2}+3=0$.
5. Find the radius and the center of the circle that is the graph of the equation $4 x^{2}+4 y^{2}+4 x-16 y=7$.
6. If $f(x)=a x^{4}-b x^{2}+x+5$ and $f(-3)=2$, then what is $f(3)$ ?
7. For how many positive integers $b$ is $\log _{b} 729$ a positive integer?
8. For what real values of $x$ is $(1-|x|)(1+x)$ positive?
9. A rubber ball is dropped from a 100 ft tall building. Each time it bounces, it rises to three-quarters its previous height. So, after its first bounce it rises to 75 ft , and after its second bounce it rises to $3 / 4$ of 75 ft , and so on forever. What is the total distance the ball travels?
10. Find all solutions to the equation $\sqrt[3]{x^{3}-x^{2}-10}=x-1$.

The answers to Do You Know Introduction to Algebra are below.

1. Oranges weigh 1 unit, apples weigh 5 units, and bananas weigh 2 units.
2. $x^{4}-x^{3} y+x^{2} y^{2}-x y^{3}+y^{4}$
3. -1
4. $\sqrt{3}, 1,-1$, and $-\sqrt{3}$
5. The radius is $\sqrt{6}$ and the center is $\left(-\frac{1}{2}, 2\right)$.
6. 8
7. There are 4 such integers: $3,9,27,729$.
8. It is positive when $x<-1$ or $-1<x<1$.
9. 700 ft
10. $3,-3 / 2$
