

ANSWER: a. Sample: The sums of the diagonals are different by 1. Moving right or down increases the number by the heading of that column or row. **b.** Answers will vary. **c.** Answers will vary.

COMMENTS & EXTENSIONS: Do the same observations hold for a 3×3 square? For example, for this 2×2 , the sums along the two diagonals (10 + 18 and 15 + 12) differ by 1. Is this true with a 3×3 square?

Make a 3×3 multiplication square. What observations do you notice about this square? How do these observations differ from your observations of the 2×2 square?

Multip	olicative Comparison	Name	Answer Key
Try This	S		
	weighs 3 pounds. My dog weigh: How much does my dog weigh?		es as much as
■ Use C	Cuisenaire Rods to model the pro	blem.	
 Draw 	your model.		
 Write 	an equation to show the answer.	•	
 Write 	the answer.		
Cat: [lt green		
Dog:	It green It green It green It gree	en It gr	een
[orange w	www	/ W
Equatio	on: 5 × 3 = 15	Mv da	g weighs 15 pounds.

1. Jackson ran 4 laps at the track on Monday. On Wednesday, he ran 3 times as many laps. How many laps did he run on Wednesday?

Monday:	purple				
Wednesday:	purple	purple	purple		
	C	orange	w w		
Equation:	3 × 4 = 12		Jackson ran _	12	laps on Wednesday.

2. This month, Debbie saved two times as much money as she saved last month. Last month she saved \$8. How much did she save this month?



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Multiplicative Comparison

3. This week Andrea ate 4 times as many apples as she ate last week. Last week she ate 2 apples. How many apples did she eat this week?

Last week:	red
This week:	red red red red brown
Equation:	4 × 2 = 8
Andrea ate _	⁸ apples this week.

4. A ribbon is 6 centimeters long. A piece of yarn is 3 times as long. How long is the piece of yarn?

Ribbon:	dark green							
Yarn:	dark green	dark gree	en		dark	gre	en	
	orange		ww	w	ww	w	w	w
Equation:	3 × 6 = 18							
The piece of yarn is <u>18</u> centimeters long.								

Solve the problem. Write an equation and the answer.

5. Sheldon is 7 years old. His father is 6 times as old as he is. How old is his father?

Equation:	6 × 7 =	42	
Sheldon's father is _	42 y	ears old.	

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Multiplicative Comparison

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Name Answer Key

6. Raj has 5 times as many baseball cards as Joey. If Joey has 8 cards, how many does Raj have?

Equation: _____5 × 8 = 40

Raj has <u>40</u> baseball cards.

7. Lena has 9 nickels. Mari has 7 times as many. How many nickels does Mari have?

Equation: $7 \times 9 = 63$

Mari has <u>⁶³</u> nickels.



Use Cuisenaire Rods to build the model. Use the model to complete the problem.

1. Amy has 2 cats. Her friend has 3 times as many cats. How many cats does Amy's friend have?



2. Bonita has two times as many pets as Tom. If Tom has 8 pets, how many pets does Bonita have?

Tom:	brown	
Bonita:	brown	brown
	orange	w w w w w w
Equation:	2 × 8 = 16	Bonita has ¹⁶ _ pets.

Use Cuisenaire Rods to model the problem. Draw your model. Use the model to complete the problem.

3. Ann is 5 years old. Her brother is 3 times as old. How old is Ann's brother?

Ann's age:	yellow			
Brother's age:	yellow	yellow	yellow	
	orar	nge	wwwww	
Equation:	3 × 5 = 15	Ann's	brother is	years old.



4. Darden picked 3 apples. Jack picked 7 times as many apples. How many apples did Jack pick?

Darden:	lt green		
Jack:	It green It green It green It	green It green It green It green]
	orange	orange w]
Equation:	7 × 3 = 21		
Jack picke	ed apples.		

Write an equation that tells the answer to the problem.

5. Over the summer, Nelly read 9 books. Sam read 4 times as many books. How many books did Sam read?

Equation: $4 \times 9 = 36$

6. Brandon's tomato plant is 4 feet tall. His corn plant is two times as tall as his tomato plant. How tall is his corn plant?

Equation:	2 × 4 = 8	
		_

7. Luke has lived in Suntown for 6 years. His mother has lived in Suntown for 5 times as many years. How many years has Luke's mother lived in Suntown?

Equation: $5 \times 6 = 30$



ANSWER: a. 2 buses; b. 3 vans

COMMENTS & EXTENSIONS: The National Assessment of Educational Progress (NAEP) has used questions like this for children around 13 years old. Many children used rote techniques and thus gave unrealistic answers. A good practice is to check one's answer within the real-life context of the problem. And make sure there are no fractional vehicles!

A school bus holds 34 students and 1 driver. Draw a bird's eye view of the bus seats. [Do not forget the driver's seat]



Try This

A tree is 24 feet tall. It is 6 times as tall as Penny. How tall is Penny?

- Build a model using Cuisenaire Rods.
- Draw your model.
- Give the answer and write an equation.

Think: The tree is 24 feet tall.

Coperations, Word Problems, and Reasoning

Lesson 2



1. There are 20 monkeys in a zoo. There are 4 times as many monkeys as tigers. How many tigers are there?

Monkeys:	orar	nge	orang	ge
	yellow	yellow	yellow	yellow
Tigers:	yellow			
There are _	⁵ _ tigers.	Equation:	$20 = 4 \times 5$, or 2	$20 \div 4 = 5$

2. A single rose costs \$2 and a bunch of roses costs \$12. How many times as much as a single rose does a bunch of roses cost?

Single rose:	red	
Bunch of roses:	orange w w	
	red red red red red	
A bunch of roses	s costs6 times as much as a single rose.	
Equation:	$12 = 6 \times 2$, or $12 \div 2 = 6$	continued on the next pac

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3. A factory has 3 times as many workers as a grocery store. The grocery store has 7 workers. How many workers does the factory have?

Grocery store:		black					
Factory:		black	b	lack		black	
		orange			orange	e	w
The factory has	21	workers. Eq	uation:	з	8 × 7 = 21		

4. A large pizza costs \$24, which is 3 times as much as a personal pizza. How much does a personal pizza cost?

Large pizza:	orange	orang	ge wwwww
U 1			
	brown	brown	brown
Personal pizz	a: brown		
A personal p	izza costs \$ <u>8</u> .		
Equation:	$3 \times 8 = 24$, or $24 \div 3 = 8$		

5. A piece of string is 9 centimeters long. A piece of wood is 18 centimeters long. How many times as long is the piece of wood compared with the piece of string?

•	0	
String:	blue	
Wood:	orange	
	blue	blue
The piece of	wood is <u></u> times as long	g as the piece of string.
Equation:	$18 = 2 \times 9$, or $18 \div 9 = 2$	



6. Paolo has 6 coins in his coin collection. Roberta has 3 times as many coins as Paolo. How many coins does Roberta have?

Paolo:	dark green		
Roberta:	dark green	dark green	dark green
	orange	ww	w w w w w w
Roberta has	18 coins.		
Equation:	3 × 6 = 18		

Write an equation and answer the question.

7. You read 5 times as long today as you read yesterday. If you read for 50 minutes today, how long did you read yesterday?

	Equation:	$50 = 5 \times 10$, or $50 \div 5 = 10$
	Answer:	10 minutes
8.	Becki saved \$32	2 this month. Last month she saved \$8.
	This month Bec	ki saved <u>4</u> times as much as she did last month.
	Equation:	$32 = 4 \times 8$, or $32 \div 8 = 4$
	Answer:	4 times as much

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Use Cuisenaire Rods to build the model. Use the model to solve the problem. Write an equation.

A rubber band was 4 centimeters long. Then it was stretched to 1. 12 centimeters. How many times as long is the rubber band when it is stretched as it was before it was stretched?

Before stretched: purple After stretched: orange w W purple purple purple

The rubber band is $\frac{3}{100}$ times as long as it was. Equation: $12 = \frac{3}{2} \times 4$, or $12 \div 4 = \frac{3}{2}$

Juan picked 20 apples. He picked 5 times as many as Gus. How many 2. apples did Gus pick?

Juan:	orange		orange			
	purple	purple	pur	ple	purple	purple
Gus:	purple					
Gus picked 4 apples. Equation: 20 = 5 × 4 , or 20 ÷ 5 = 4 Build a model for the problem. Draw your model for each part. Solve the problem, and write an equation.						

Models may vary.



Multiplicative Comparison Problems

Name Answer Key

3. A pack of pencils costs 7 times as much as one pencil. One pencil costs 3 cents. How much does a pack of pencils cost?

One pencil: It green Pack of pencils: It green orange orange W A pack of pencils costs _____ cents. $7 \times 3 = 21$ Equation: The giraffe at the zoo is 16 feet tall, which is 4 times as tall as the 4. chimpanzee. How tall is the chimpanzee? Giraffe: orange w |w |w |w | w w purple purple purple purple

Chimpanzee: The chimpanzee is $\frac{4}{16 = 4 \times 4$, or $16 \div 4 = 4$

Write an equation to solve the problem.

5. Andre and Zach went fishing. Zach caught 28 fish. He caught 7 times as many fish as Andre. How many fish did Andre catch?

Equation: $28 = 7 \times 4$, or $28 \div 7 = 4$ Andre caught 4 fish.

6. Shelly and Vicky collect stickers. Vicky has 5 times as many stickers as Shelly. If Vicky has 40 stickers, how many stickers does Shelly have?

Equation: $40 = 5 \times 8$, or $40 \div 5 = 8$ Shelly has 8 stickers. © ETA hand2mind®



Andy is half as old as his dad.

His dad is 42.

How old will Andy be when his dad is 50?

ANSWER: 29 years old

COMMENTS & EXTENSIONS: This is a question that requires students to determine not only what information is relevant, but in what manner and at what time it is relevant. Half is relevant only for the current year, as Andy will not be 25 when his dad is 50. Dozens of similar questions can be generated by changing the word "half," the number 42, and the number 50.

 $\mathcal{F}_{\gamma\gamma\gamma}^{\gamma\gamma\gamma}$ Quinn is one quarter as old as his dad. His dad is 44. How old will Quinn be when his dad is 45?



Multistep Problems I

Name Answer Key

Try This

Sal bought 2 boxes of erasers. Each box contained 9 erasers. He gave 5 of the erasers to his sister. How many does he have now?

- Estimate the answer.
- Use Color Tiles or Base Ten Blocks to model the problem.
- For each step, draw your model and write an equation.



1. Tara has 12 fruit cups and 15 pudding cups for the party. She will put equal numbers of cups on each of 3 serving trays. How many will she put on each tray?





2. A pizza shop made 4 pepperoni pizzas, 11 cheese pizzas, and 6 veggie pizzas. If the 3 cooks each made the same number of pizzas, how many pizzas did each cook make?



3. Mrs. Hitte gave her 3 children \$30 to share equally. Her son wants to buy 5 bags of marbles. If each bag costs \$2, does he have enough money?



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4. There are 15 students in Mrs. Small's class. There are 17 students in Mrs. Little's class. Both classes are attending a play together. Each table at the play seats 4 children. How many tables are needed?

Estimate:	Answers will vary.		
• •	Models will vary.	•••••	Models will vary.
	15 + 17 = 32	** * * * * * * *	32 ÷ 4 = 8
Answer:	8 tables are	e needed.	

For each problem, estimate the answer. Write the equations you use to solve the problem, and write the answer.

5. Andrew discovered a buried treasure box. He opened it and found that it contained 12 diamonds and 22 rubies. The owner of the box gave Andrew 9 of the gems as a reward for returning it. How many gems did the owner keep?

Estimate:	Answers will vary.		
Equations:	12	+ 22 = 34	
	34	- 9 = 25	
Answer:	The owne	er kept 25 gems.	

6. Jenna has 13 hardcover books and 29 paperback books. She is packing them in boxes. Each box can hold 7 books. How many boxes will she need?

Estimate:	Answers will vary.	
Equations:	13 + 29 = 42	
	42 ÷ 7 = 6	
Answer:	Jenna will need 6 boxes.	

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Estimate the answer to the problem. Use Color Tiles to build the models, and use the models to complete the equations and the answer.

A family is going to the museum. The family has 2 adults and 1. 2 children. Each adult's ticket costs \$5, and each child's ticket costs \$3. How much will the family pay for all their tickets?

Estimate: Answers will vary.	
Step 1:	Step 2:
Think: 2 adults, \$5 each.	Think: 2 children, \$3 each.
Equation: $2 \times 5 = $ <u>10</u>	Equation: $2 \times 3 = \frac{6}{2}$
Think: How much in all?	
Equation: $10 + 6 = 16$	
Answer: The family will pay for all the	ir tickets.

Estimate the answer, then use Color Tiles or Base Ten Blocks to build models for the problem. Sketch your models and use them to write equations. Give the answer.

Larry's friend gave him \$20. He used the money to buy 5 packs of 2. baseball cards for \$3 each. How much money does Larry have left?



3. Eva's desk drawer contains pencils and pens. There are 4 pencils. There are 6 more pens than pencils. How many pencils and pens are there in all?



4. There are 14 students in Mrs. Smart's class. There are 16 students in Mr. Lee's class. The classes are going to the library together for reading time. Each table at the library seats 5 children. How many tables are needed?

Estimate:	Answers will var	у.	
	Models will vary 14 + 16 = 30		Models will vary. $30 \div 5 = 6$
Answer:	6 t	ables are needed.	



For each problem, estimate the answer. Write the equations you use to solve the problem, and write the answer.

5. There are 5 football games each month. The season is 4 months long. If the team won 11 games, how many did it lose?

Estimate:	Answers will vary.	
Equations:	4 × 5 = 20	
	20 - 11 = 9	
Answer:	The team lost 9 gam	nes.

6. On Monday, Mickey bought 2 packs of animal cards. On Tuesday, he bought 4 packs. Each pack has 9 cards. He gave 19 cards to his friend. How many cards does Mickey have left?

Estimate:	Answers will vary.		
Equations:	(2 × 9)	+ (4 × 9) = 54	
	54	- 19 = 35	
Answer:	Mickey ha	as 35 cards left	



ANSWER: Example: Fill the 5-liter container; pour it into the 4-liter container, leaving 1 liter. Put this 1 liter into the 10-liter container. Empty the 4-liter container and repeat this process to put a second liter in the 10-liter container. There are more ways.

COMMENTS & EXTENSIONS: Set other targets for children using the 5-liter, 4-liter, and 10-liter containers. Here is another challenge: you have a 2-liter container, a 7-liter container, and an infinite supply of fluid. Using the containers, what measurements can you get?

Try This

Emily had 6 flowers. Then she bought 9 more flowers from a florist. She will give the same number of flowers to each of her 2 teachers. How many flowers can she give each teacher?

- Choose a tool and build a model.
- For each step in the problem, draw your model and write an equation.
- Give the answer.



 Jackie baked 3 trays of 10 muffins. After they cooled, she divided them equally into 4 bags. How many muffins did she put in each bag?



Multistep Problems II

Coperations, Word Problems, and Reasoning

Lesson 4

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Name Answer Key

2. A teacher has 5 bags of marbles. Two of the bags have 4 marbles in them. The other 3 bags have 5 in them. How many marbles are there in all?



3. Mr. Little divided \$27 equally among his 3 children. His daughter, Lisa, used her money to buy 3 gifts. If each gift cost the same amount. What was the price of each gift?

27 ÷ 3	3 = 9	S	$9 \div 3 = 3$	
Answer: _ <mark>\$3</mark> _				

4. You earn \$4 for each hour of babysitting and \$3 for each hour of weeding the garden. Last week you did 4 hours of babysitting and 3 hours of weeding. How much more did you earn babysitting than you earned weeding?

		3 × 3 = 9	
Answer:	4 × 4 = 16		16 – 9 = 7
			continued on the next

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Solve the problem. Write equations and give the answer.

5. Michael had 22 books and got 9 more for his birthday. If each of his cubbies can hold 6 books, how many cubbies does Michael need for his books? Explain.



Answer: 5 cubbies can hold only 30 books, so Michael needs one more.

- 6. DVDs are on sale for \$4. Books are on sale for \$3. You want to buy 5 DVDs and 4 books. If you have \$35, do you have enough money? Explain.
 - $5 \times 4 = 20$ $4 \times 3 = 12$ 20 + 12 = 32

Answer: Yes. The DVDs and books cost \$32, which is less than \$35.

Use Centimeter Cubes to build the model. Use the model to complete the problem.

1. Jenny wants to buy 3 books that cost \$5 each. She gets paid \$4 to walk a dog. If she walks 4 dogs, will she earn enough to buy the books?

Step 1:	Step 2:	
Equation: $3 \times 5 = \frac{15}{2}$	Equation: $4 \times 4 = $	
Answer:		
Yes, she has enough money; she will earn \$16, which is more than \$15.		

2. Tabitha bought 3 boxes of fish food and 2 packets of cat food. Each box of fish food contains 4 pouches, and each packet of cat food contains 3 pouches. How many more pouches of fish food than cat food did Tabitha buy?

Step 1:		Step 2:
Equation: 3 × 4 =	_ 12	Equation: $2 \times 3 = $
Step 3:		
Equation: 12 – 6	=6	
Answer:		
	Tabitha bought 6 more pouches of f	fish food than cat food.



Use Centimeter Cubes to model the problem. Draw your models, write equations, and give the answer.

3. Raul has 23 tins and a case that has 9 shelves. Six of the shelves can hold only 2 tins. Three shelves can hold only 3 tins. Can he fit all the tins on the 9 shelves? Explain.



4. Cameron bought 6 bottles of water to add to the 16 bottles he already had. Now he wants to divide the water equally between 4 friends. How many bottles can each friend get?





Write equations for the problem and give the answer.

5. Cecile bought 2 pairs of flip-flops that cost \$8 each and a pair of tennis shoes that cost \$22. How much did she pay for her flip-flops and tennis shoes together?

2 × 8 = 16
16 + 22 = 38

Answer: ______

6. Maria picked 9 red flowers and 8 yellow flowers from her garden. If each vase can hold only 5 flowers, how many vases does she need?

